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Centre Number				Candidate Number					
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**Pearson Edexcel Level 3 GCE**

**Monday 26th June 2023**

Afternoon (Time: 1 hour 30 minutes) **Paper reference** **9FM0/4C**

**Further Mathematics**

**Advanced**

**PAPER 4C: Further Mechanics 2**

**You must have:**  
Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.  
Answers without working may not gain full credit.
- Unless otherwise indicated, whenever a value of  $g$  is required, take  $g = 9.8 \text{ m s}^{-2}$  and give your answer to either 2 significant figures or 3 significant figures.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1. Three particles of masses  $3m$ ,  $4m$  and  $km$  are positioned at the points with coordinates  $(2a, 3a)$ ,  $(a, 5a)$  and  $(2\mu a, \mu a)$  respectively, where  $k$  and  $\mu$  are constants.

The centre of mass of the three particles is at the point with coordinates  $(2a, 4a)$ .

Find (i) the value of  $k$

(ii) the value of  $\mu$

(6)

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2. A particle of mass 2 kg is moving in a straight line on a smooth horizontal surface under the action of a horizontal force of magnitude  $F$  newtons.

At time  $t$  seconds ( $t > 0$ ),

- the particle is moving with speed  $v \text{ ms}^{-1}$
- $F = 2 + v$

The time taken for the speed of the particle to increase from  $5 \text{ ms}^{-1}$  to  $10 \text{ ms}^{-1}$  is  $T$  seconds.

(a) Show that  $T = 2 \ln \frac{12}{7}$  (4)

The distance moved by the particle as its speed increases from  $5 \text{ ms}^{-1}$  to  $10 \text{ ms}^{-1}$  is  $D$  metres.

(b) Find the exact value of  $D$ . (4)

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3. [In this question you may quote, without proof, the formula for the distance of the centre of mass of a uniform circular arc from its centre.]

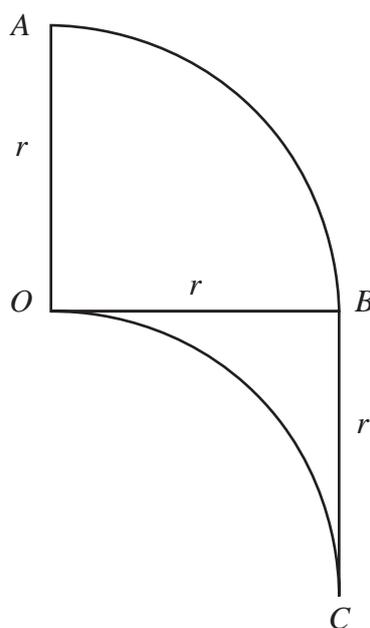


Figure 1

Five pieces of a uniform wire are joined together to form the rigid **framework**  $OABCO$  shown in Figure 1, where

- $OA$ ,  $OB$  and  $BC$  are straight, with  $OA = OB = BC = r$
- arc  $AB$  is one quarter of a circle with centre  $O$  and radius  $r$
- arc  $OC$  is one quarter of a circle of radius  $r$
- all five pieces of wire lie in the same plane

- (a) Show that the centre of mass of arc  $AB$  is a distance  $\frac{2r}{\pi}$  from  $OA$ . (2)

Given that the distance of the centre of mass of the framework from  $OA$  is  $d$ ,

- (b) show that  $d = \frac{7r}{2(3 + \pi)}$  (4)

The framework is freely pivoted at  $A$ .

The framework is held in equilibrium, with  $AO$  vertical, by a horizontal force of magnitude  $F$  which is applied to the framework at  $C$ .

Given that the weight of the framework is  $W$

- (c) find  $F$  in terms of  $W$  (3)

































7.

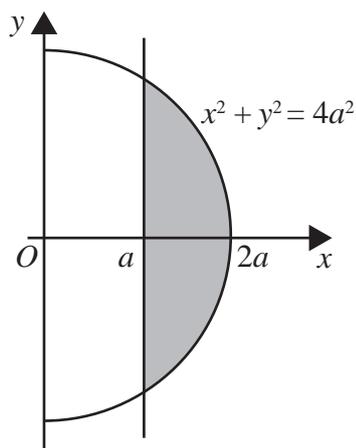


Figure 5

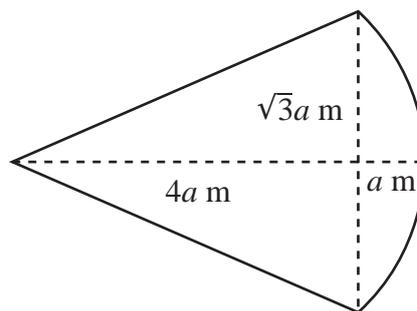


Figure 6

The shaded region shown in Figure 5 is bounded by the line with equation  $x = a$  and the curve with equation  $x^2 + y^2 = 4a^2$

This shaded region is rotated through  $180^\circ$  about the  $x$ -axis to form a solid of revolution.

This solid is used to model a dome with height  $a$  metres and base radius  $\sqrt{3}a$  metres.

The dome is modelled as being non-uniform with the mass per unit volume of the dome at the point  $(x, y, z)$  equal to  $\frac{\lambda}{x^2}$   $\text{kg m}^{-3}$ , where  $a \leq x \leq 2a$  and  $\lambda$  is a constant.

- (a) Show that the distance of the centre of mass of the dome from the centre of its plane face is  $\left(4 \ln 2 - \frac{5}{2}\right)a$  metres.

(6)

A solid uniform right circular cone has base radius  $\sqrt{3}a$  metres and perpendicular height  $4a$  metres. A toy is formed by attaching the plane surface of the dome to the plane surface of the cone, as shown in Figure 6.

The weight of the cone is  $kW$  and the weight of the dome is  $2W$

The centre of mass of the toy is a distance  $d$  metres from the plane face of the dome.

- (b) Show that  $d = \frac{|k + 5 - 8 \ln 2|}{2 + k}a$

(4)

The toy is suspended from a point on the circumference of the plane face of the dome and hangs freely in equilibrium with the plane face of the dome at an angle  $\alpha$  to the downward vertical.

Given that  $\tan \alpha = \frac{1}{2\sqrt{3}}$

- (c) find the exact value of  $k$ .

(3)

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8.

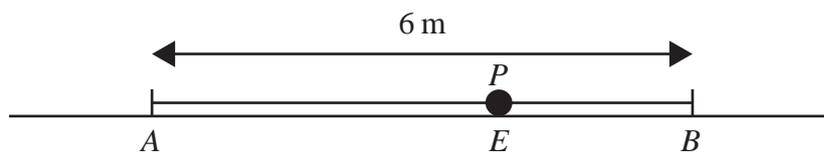


Figure 7

The fixed points  $A$  and  $B$  lie on a smooth horizontal surface with  $AB = 6$  m.

A particle  $P$  has mass  $0.3$  kg.

One end of a light elastic string, of natural length  $2$  m and modulus of elasticity  $20$  N, is attached to  $P$ , and the other end is attached to  $A$ .

One end of another light elastic string, of natural length  $2$  m and modulus of elasticity  $40$  N, is attached to  $P$  and the other end is attached to  $B$ .

The particle  $P$  is at rest in equilibrium at the point  $E$  on the surface, as shown in Figure 7.

- (a) Show that  $EB = \frac{8}{3}$  m. (3)

The particle  $P$  is now held at the midpoint of  $AB$  and released from rest.

- (b) Show that  $P$  oscillates with simple harmonic motion about the point  $E$ . (4)

The time between the instant when  $P$  is released and the instant when it first returns to the point  $E$  is  $S$  seconds.

- (c) Find the exact value of  $S$ . (3)

- (d) Find the length of time during one oscillation for which the speed of  $P$  is more than  $2$  m s<sup>-1</sup>. (4)

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